



# UNIVERSITÀ DI PAVIA

Anno Accademico 2018/2019

## FOUNDATIONS OF MECHANICS

|                            |   |
|----------------------------|---|
| <b>Enrollment year</b>     | 2017/2018   |
| <b>Academic year</b>       | 2018/2019   |
| <b>Regulations</b>         | DM270   |
| <b>Academic discipline</b> | MAT/07 (MATHEMATICAL PHYSICS)   |
| <b>Department</b>          | DEPARTMENT OF MATHEMATICS "FELICE CASORATI"   |
| <b>Course</b>              | MATHEMATICS   |
| <b>Curriculum</b>          | PERCORSO COMUNE   |
| <b>Year of study</b>       | 2°  |
| <b>Period</b>              | 2nd semester (04/03/2019 - 14/06/2019)  |
| <b>ECTS</b>                | 9   |
| <b>Lesson hours</b>        | 84 lesson hours   |
| <b>Language</b>            | Italian   |
| <b>Activity type</b>       | WRITTEN AND ORAL TEST   |
| <b>Teacher</b>             | PULVIRENTI ADA (titolare) - 9 ECTS  |
| <b>Prerequisites</b>       | Analysis 1, Analysis 2, Geometry 1 and Linear Algebra.  |
| <b>Learning outcomes</b>   | The aim of the course is to present the basic mathematical models of classical mechanics, in their theoretical aspects and in their applications.   |
| <b>Course contents</b>     | Kinematics of a point.<br>Dynamics: fundamental principles.<br>The motion of a free particle.<br>Constraints.<br>Multi particles systems.<br>Rigid systems.<br>Cardinal equations of dynamics.<br>Lagrange's equations.<br>Some classical problems: the problem of two bodies.<br>Equilibrium and stability.<br>Hamilton's principle. |

Hamilton's equations.  
Canonical transformations. Poisson brackets.

Extended summary

Kinematics of a point. Frenet's frame.  
Constraints and their classification.  
The motion of a free particle.  
Lagrangian coordinates.  
Dynamics: the fundamental principles of mechanics.  
Work and energy. Conservative forces.  
The motion of a point under constraint.  
Discrete systems. Cardinal equations of dynamics. Non dissipative constraints.  
Lagrange's equations. Lagrange's equations for conservative systems.  
Conservation laws.  
One-dimensional motions. Qualitative analysis.  
Some classical problems: the problem of two bodies. Kepler's equations.  
Rigid body: Euler's angles. Angular velocity. Relative motions.  
Rigid body dynamics: inertia ellipsoid. Euler's equations. Lagrange's gyroscope.  
Equilibrium and stability: Lagrange-Dirichlet theorem. Instability criteria.  
Small oscillations.  
Variational principles of mechanics: Hamilton's principle.  
The Hamiltonian function (via Legendre transformation). Hamilton's equations.  
Canonical transformations. Poisson brackets.

**Teaching methods**

Lectures and exercises.

**Recommended or required readings**

1. Fasano A., Marmi S.: "Meccanica Analitica", Bollati Boringhieri.
2. Goldstein H., Poole C., Safko J.: "Meccanica Classica", Zanichelli.
3. Gantmacher F.R.: "Lezioni di Meccanica Analitica", Editori Riuniti.
4. Lanczos C., : "The variational principles of Mechanics, Dover.

**Assessment methods**

Written and oral examination.

**Further information**

Written and oral examination.

**Sustainable development goals - Agenda 2030**

[Sbl legenda sviluppo sostenibile](#)