



### FOUNDATIONS OF MECHANICS

<b>Enrollment year</b>	2015/2016
<b>Academic year</b>	2016/2017
<b>Regulations</b>	DM270
<b>Academic discipline</b>	MAT/07 (MATHEMATICAL PHYSICS)
<b>Department</b>	DEPARTMENT OF MATHEMATICS "FELICE CASORATI"
<b>Course</b>	MATHEMATICS
<b>Curriculum</b>	PERCORSO COMUNE
<b>Year of study</b>	2°
<b>Period</b>	2nd semester (01/03/2017 - 09/06/2017)
<b>ECTS</b>	9
<b>Lesson hours</b>	84 lesson hours
<b>Language</b>	ITALIAN
<b>Activity type</b>	ORAL TEST
<b>Teacher</b>	PULVIRENTI ADA (titolare) - 9 ECTS
<b>Prerequisites</b>	Analysis 1, Analysis 2, Geometry 1 and Linear Algebra.
<b>Learning outcomes</b>	The aim of the course is to present the basic mathematical models of classical mechanics, in their theoretical aspects and in their applications.
<b>Course contents</b>	Kinematics of a point. Dynamics: fundamental principles. The motion of a free particle. Constraints. Multi particles systems. Rigid systems. Cardinal equations of dynamics. Lagrange's equations. Some classical problems: the problem of two bodies. Equilibrium and stability. Hamilton's principle.

Hamilton's equations.  
Canonical transformations. Poisson brackets.

Extended summary

Kinematics of a point. Frenet's frame.  
Constraints and their classification.  
The motion of a free particle.  
Lagrangian coordinates.  
Dynamics: the fundamental principles of mechanics.  
Work and energy. Conservative forces.  
The motion of a point under constraint.  
Discrete systems. Cardinal equations of dynamics. Non dissipative constraints.  
Lagrange's equations. Lagrange's equations for conservative systems.  
Conservation laws.  
One-dimensional motions. Qualitative analysis.  
Some classical problems: the problem of two bodies. Kepler's equations.  
Rigid body: Euler's angles. Angular velocity. Relative motions.  
Rigid body dynamics: inertia ellipsoid. Euler's equations. Lagrange's gyroscope.  
Equilibrium and stability: Lagrange-Dirichlet theorem. Instability criteria.  
Small oscillations.  
Variational principles of mechanics: Hamilton's principle.  
The Hamiltonian function (via Legendre transformation). Hamilton's equations.  
Canonical transformations. Poisson brackets.

**Teaching methods**

Lectures and exercises.

**Recommended or required readings**

1. Fasano A., Marmi S.: "Meccanica Analitica", Bollati Boringhieri.
2. Goldstein H., Poole C., Safko J.: "Meccanica Classica", Zanichelli.
3. Gantmacher F.R.: "Lezioni di Meccanica Analitica", Editori Riuniti.
4. Lanczos C., : "The variational principles of Mechanics, Dover.

**Assessment methods**

Written and oral examination.

**Further information**

Written and oral examination.

**Sustainable development goals - Agenda 2030**

[Sbl legenda sviluppo sostenibile](#)